## ACSC/STAT 4703, Actuarial Models II

## FALL 2024

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#### Homework Sheet 3

#### Due: Thursday 3rd Octomber: 11:30

### **Basic Questions**

1. Loss amounts follow a gamma distribution with shape  $\alpha = 3.4$  and scale  $\theta = 700$ . The distribution of the number of losses is given in the following table:

Number of Losses	Probability
0	0.750
1	0.114
2	0.085
3	0.051

Assume all losses are independent and independent of the number of losses. The insurance company buys excess-of-loss reinsurance on the part of the loss above \$7,000. Calculate the expected payment for this excess-of-loss reinsurance.

2. Loss frequency follows a negative binomial distribution with r = 7 and  $\beta = 0.25$ . Loss severity (in thousands) has the following distribution:

Severity	Probability
0	0.44
1	0.27
2	0.11
3	0.09
4 or more	0.09

Use the recursive method to calculate the exact probability that aggregate claims are at least \$4,000.

3. Use an arithmetic distribution (h = 1) to approximate a Burr distribution with  $\alpha = 3$ ,  $\gamma = 2$  and  $\theta = 1$ .

(a) Using the method of rounding, calculate the mean of the arithmetic approximation. [You can evaluate this numerically: use 5,000 terms in the sum.]

(b) Using the method of local moment matching, matching 1 moment on each interval, estimate the probability that the value is larger than 4.5.

# **Standard Questions**

4. The number of claims an insurance company receives follows a compound Poisson-negative binomial distribution with  $\lambda = 2099$  for the primary distribution and r = 0.7,  $\beta = 1.3$  for the secondary distribution. Claim severity follows a Poisson distribution with  $\lambda = 5$ . Calculate the probability that aggregate losses exceed \$10,000.

(a) Starting the recurrence 6 standard deviations below the mean [You need to calculate 15,000 terms of the recurrence for  $f_s$ .]

(b) Using a suitable convolution.